

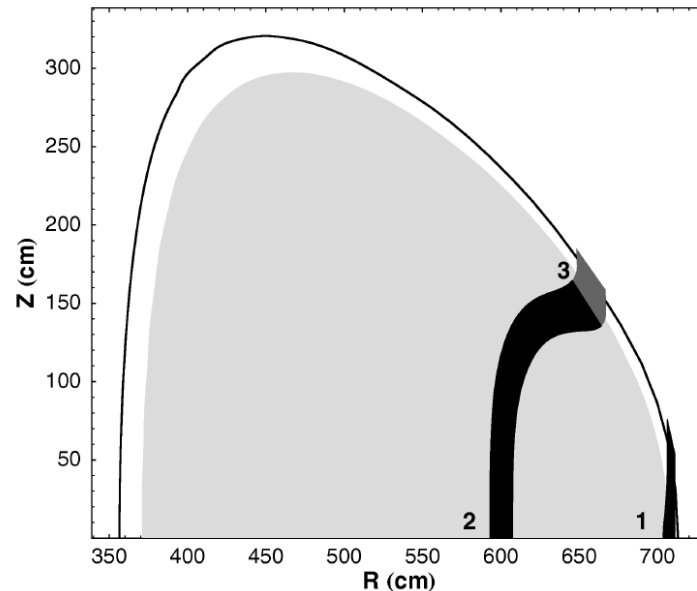
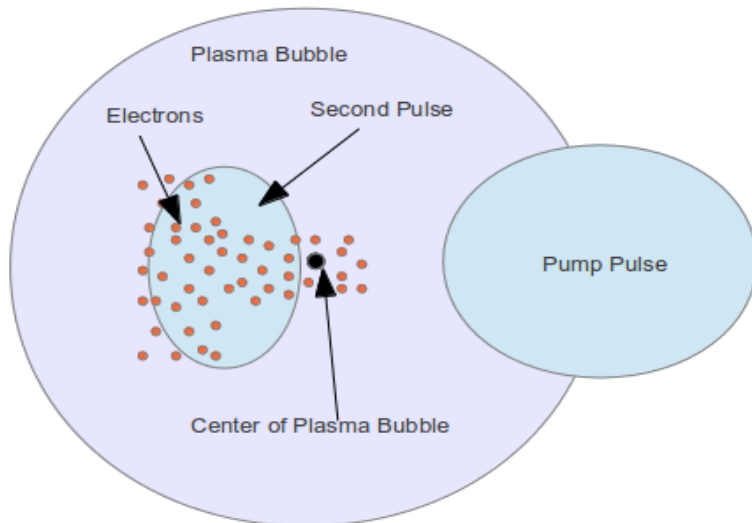


# New and Emerging Concepts in Laser-Plasma Acceleration

or

how I learned that more waves is better than fewer

Gennady Shvets, The University of Texas at Austin



Solved and Unsolved Problems in Plasma Physics, March 28, 2016



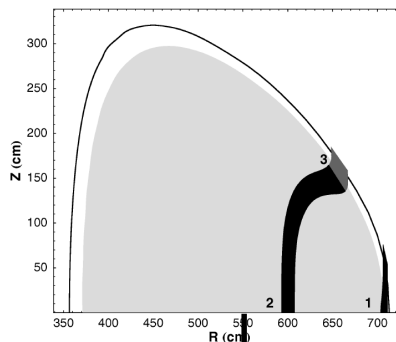
# The Timeline



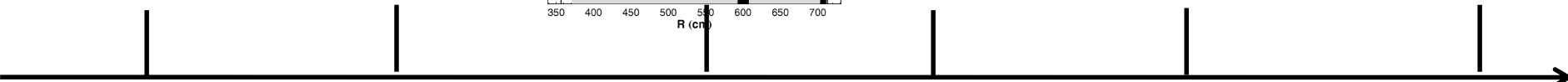
Alfven eigenmodes & ion Bernstein modes are both needed!



Automatic doors into infinite corridor existed during Nat's time there



Discover that a tokamak is not a slab → all course work with B. Coppi is invalidated



1992

1993

1995

1997

1998

2002

Meet Nat at the DPP, present an FEL poster on a concept that does not work

MIT: apply for the DOE fellowship to work on alpha channeling

$\alpha$ -channeling work starts on Feb.1, stops in March.

Trip to Nizhny Novgorod → Nat practices his Russian on me and students

Discovery of laser compression in plasma: at least three waves are needed!

...

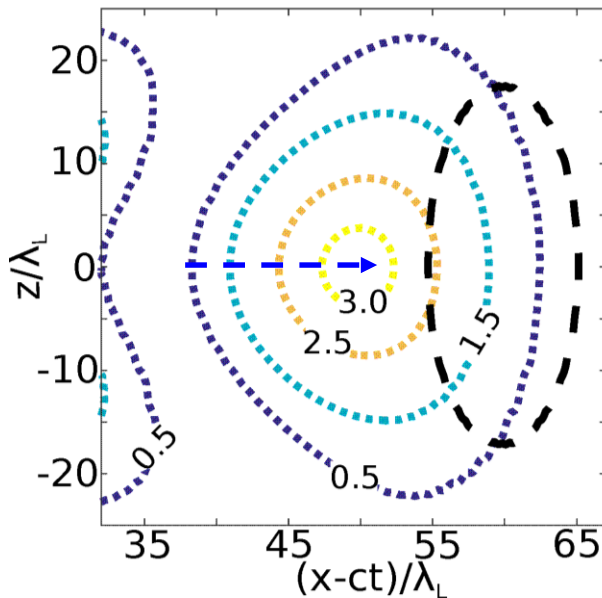
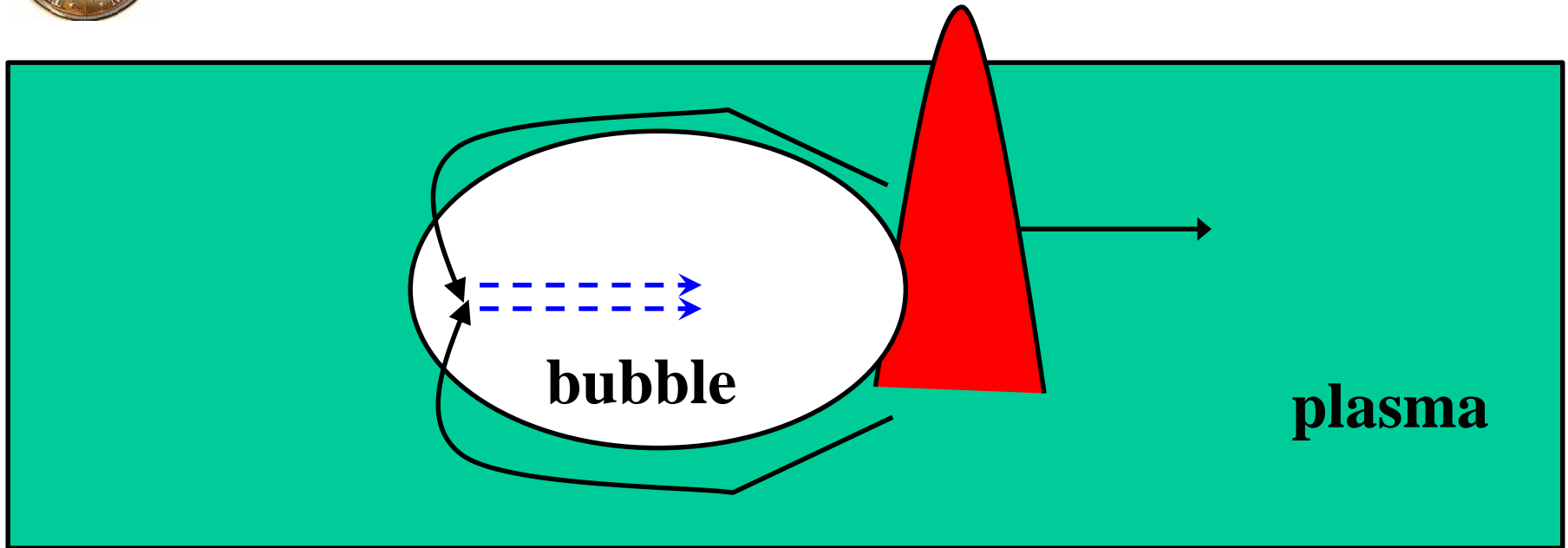
**“We’ll work on  $\alpha$ -channeling and then figure something out”**

**“Fusion is very deep but not too broad; LP is very broad but not too deep”**

**“Engineers use fluid descriptions. Physicists go into the phase space!”**



# Plasma bubble: the workhorse



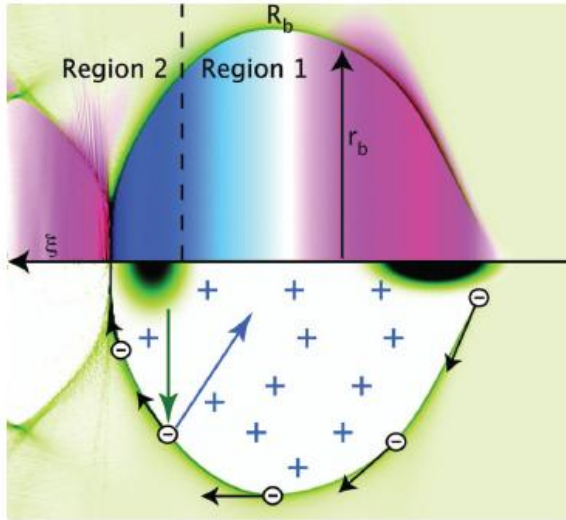
Particle advances inside bubble  $\rightarrow$  gains energy from low-frequency electric field  $\rightarrow$  energy gain is limited by dephasing

$$H_{MF} \approx \frac{p_x}{2\gamma_b^2} - \Psi \rightarrow \Delta p_x = 2\gamma_b^2 \Delta \Psi$$

Can we do better??



# Electrons motion inside the bubble and Direct Laser Acceleration



Electrons execute betatron motion with frequency  $\omega_\beta$

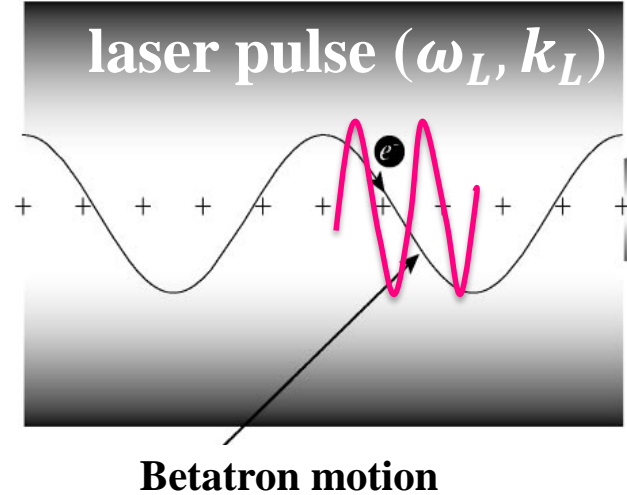
Transverse energy  $\epsilon_\perp$  is reduced due to the conservation of the action  $I_\perp = \epsilon_\perp / \omega_\beta$

Betatron frequency

$$\omega_\beta = \omega_p / (2\gamma)^{1/2}$$

Transverse energy

$$\epsilon_\perp \equiv p_\perp^2 / 2\gamma m_e + \omega_p^2 m_e^2 z^2 / 4$$



Break the adiabatic invariant by introducing an additional resonant laser pulse  $\rightarrow$  DLA

$$\omega_L - k_L v = (2n + 1) \frac{\omega_p}{\sqrt{2\gamma}}$$

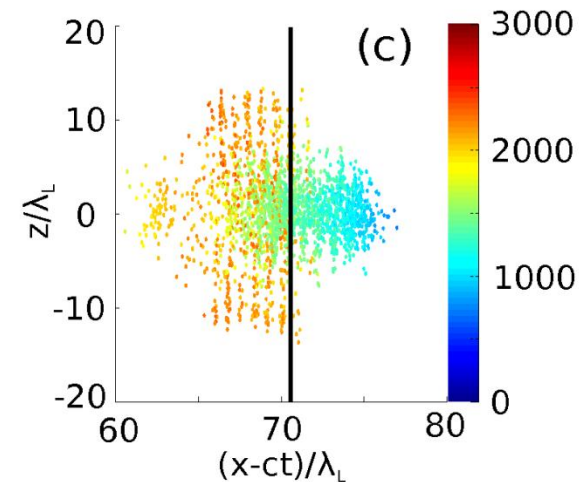
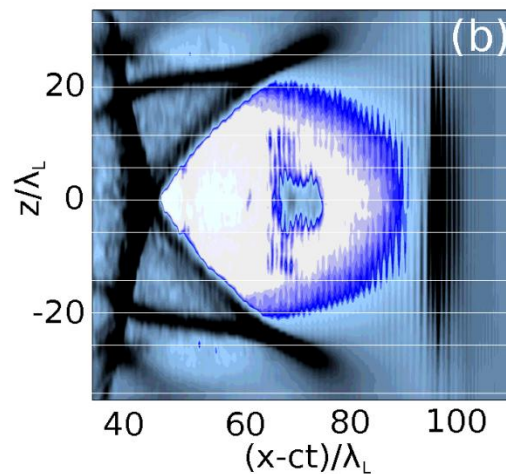
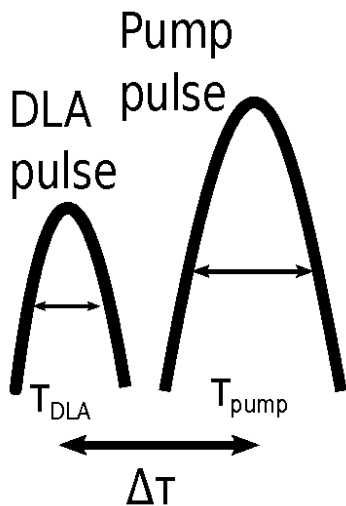
$$\Delta\gamma = \frac{\Delta\epsilon_\perp / mc^2}{1 - c/v_{ph}}$$



# Outline of the Talk



- How LWFA and DLA can work together, delay dephasing, and bifurcate the phase space
- How to inject electrons into the plasma bubble and have them experience synergistic DLA/LWFA
- Constant gradient DLA in the decelerating phase of the wake
- **Mix-and-match: combining multiple lasers for DLA + LWFA**





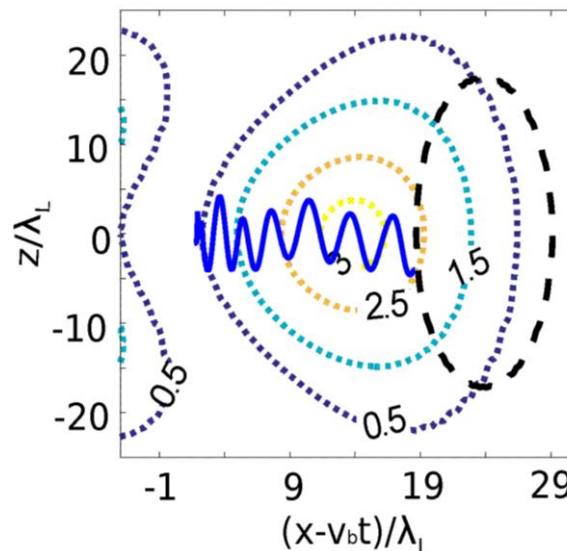
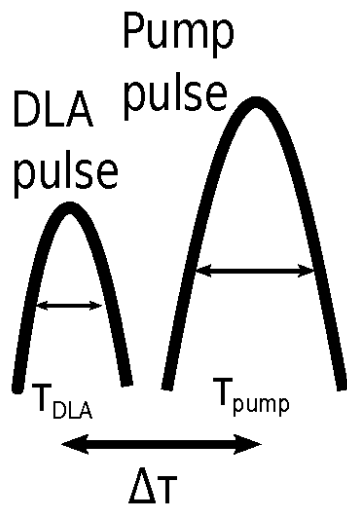
# Can LWFA and DLA work together?

- DLA's resonance condition can be undone by rapid wakefield acceleration:  $\omega_L(1 - v_x/v_{ph}) = \omega_p/\sqrt{2\gamma}$
- DLA requires large  $\vec{v}_\perp$  because  $A_L \propto \vec{v}_\perp \cdot \vec{A}_L$ , but the conservation of  $I_\perp$  reduces  $|\vec{v}_\perp|$  during acceleration!

LWFA is bad for DLA

- DLA laser pulse can distort the bubble and impede LWF acceleration or electron injection into the bubble
- Large amplitude of betatron oscillations may reduce the accelerating gradient experienced inside the bubble

DLA is bad for LWFA



**But the benefits of combining the two could be substantial!**

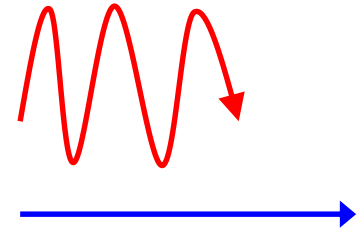
X. Zhang, V. Khudik, and GS, PRL **114**, 184801 (2015)

X. Zhang, V. Khudik, A. Pukhov, and GS, PPCF **58**, 034011 (2016)



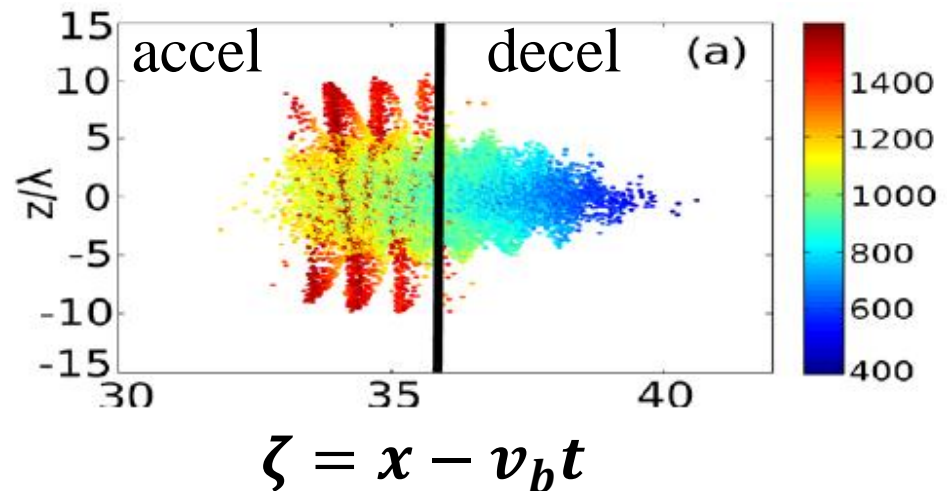
# Benefits of Synergistic Laser Wakefield & Direct Laser Acceleration

- Cumulative energy gain from LWFA and DLA
- Potentially higher energy gain from LWFA due to delayed dephasing
- Large transverse momentum  $K = p_{\perp}/mc \rightarrow$  efficient source of X-rays and  $\gamma$  -rays up to  $K^3$  harmonic of  $\omega_L$
- Combining multiple laser pulses (mid-IR + near-IR)



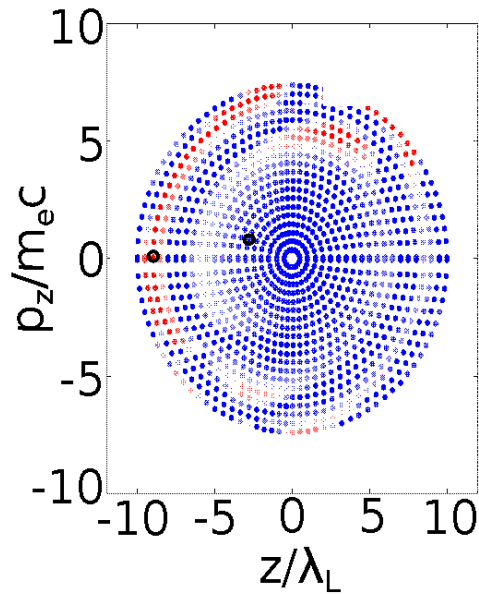
$$\frac{d\zeta}{d(ct)} \approx \frac{1}{2\gamma_b^2} - \frac{1 + \langle p_{\perp}^2/m_e^2 c^2 \rangle}{\gamma^2}$$

X. Zhang et. al., PRL **114**, 184801 (2015);  
PPCF **58**, 034011 (2016)

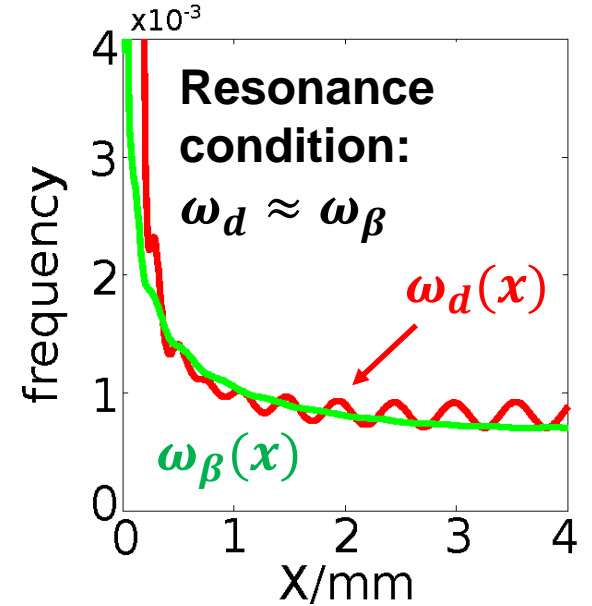
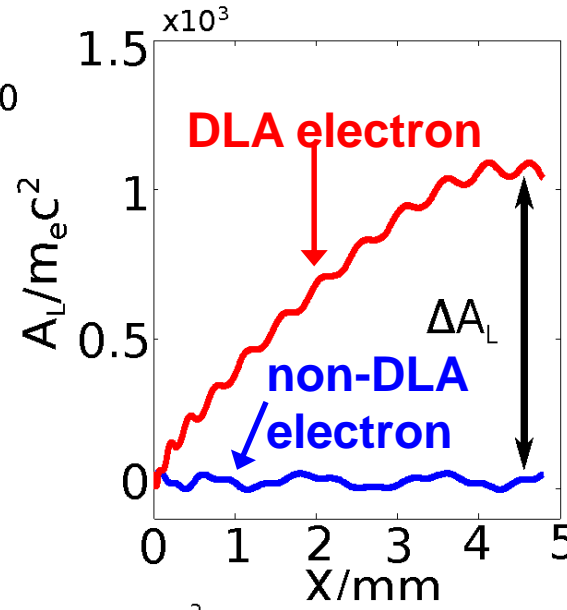




# Synergistic DLA/LWFA: single-particle simulations of a particle swarm



Swarm of initial conditions ( $p_{\perp}, r_{\perp}$ )



$$\omega_d = \omega_L \left( \frac{1 + \langle p_z^2 / m^2 c^2 \rangle}{2\gamma^2} + \frac{1}{2\gamma_{ph}^2} \right)$$

## Necessary ingredients of DLA/LWFA synergy:

- (a) electron injection with large transverse energy
- (b) strong overlap between electrons and the laser
- (c) betatron resonance between electrons and the laser





# Can DLA happen in a plasma bubble?

Pump pulse creates a bubble

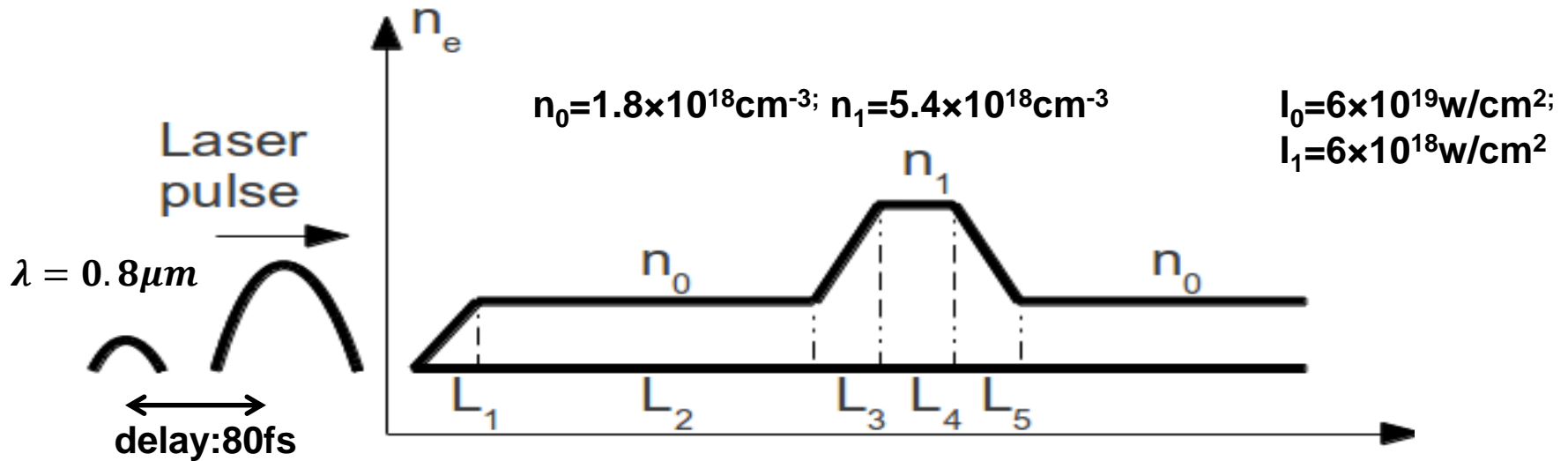
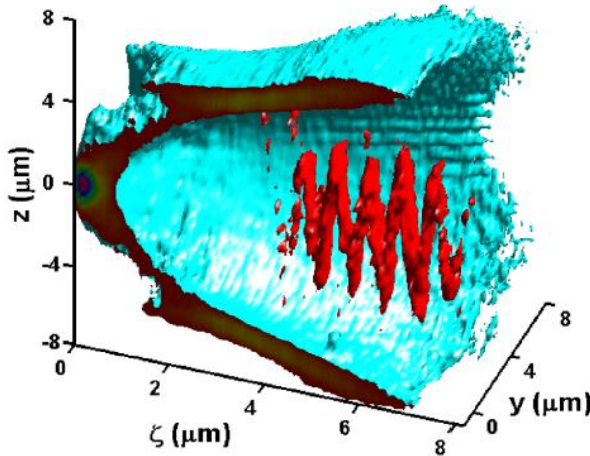


Density bump “shakes” the bubble → side-injection with large  $p_{\perp}$  → facilitates DLA



Density ramp injection scenario

Self-injected electrons interact with the weaker laser pulse delayed by  $\Delta\tau=80\text{fs}$



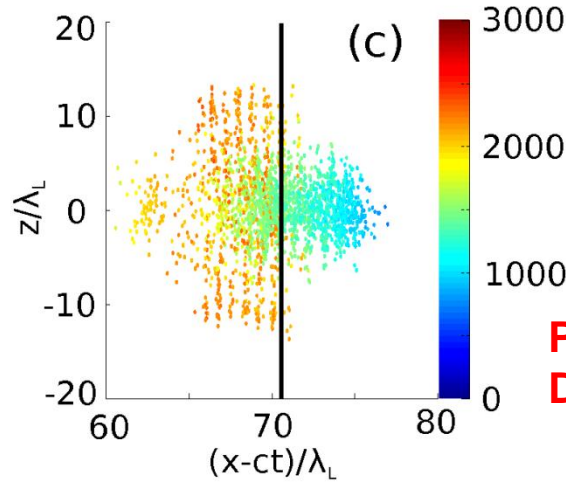
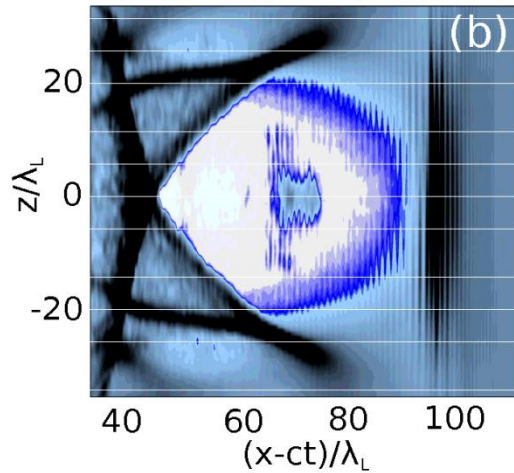
$L_2 = 1.6\text{mm}, L_3 = L_4 = L_5 \approx 100\mu\text{m}$

X. Zhang et. al. PRL 114, 184801 (2015)



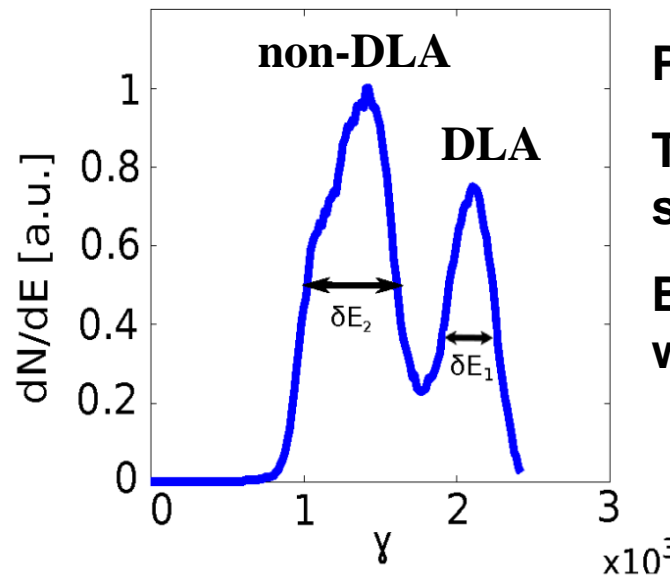
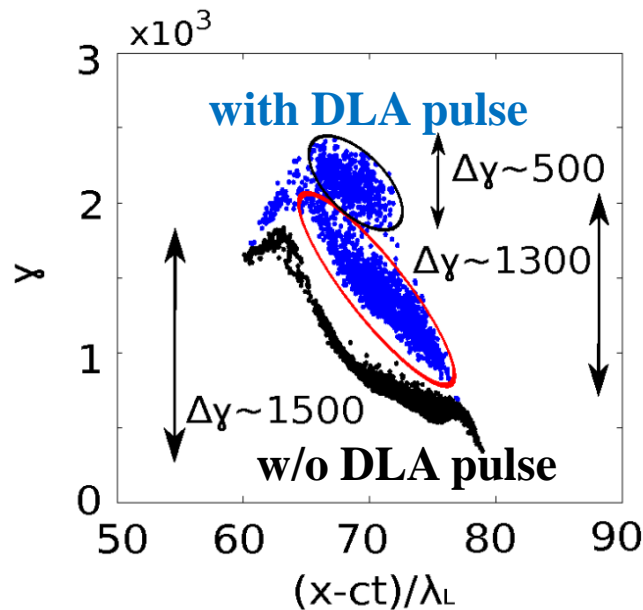
# DLA inside a plasma bubble

after 1cm propagation



Electrons separated into two groups  $\rightarrow$  DLA electrons with large  $p_{\perp}$  gain more energy and fall behind the non-DLA ones

**Pump:**  $a_L = 5.3, \tau_L = 70 \text{ fs}, w_0 = 20 \mu\text{m}$   
**DLA:**  $a_L = 1.7, \tau_L = 35 \text{ fs}, w_0 = 20 \mu\text{m}$



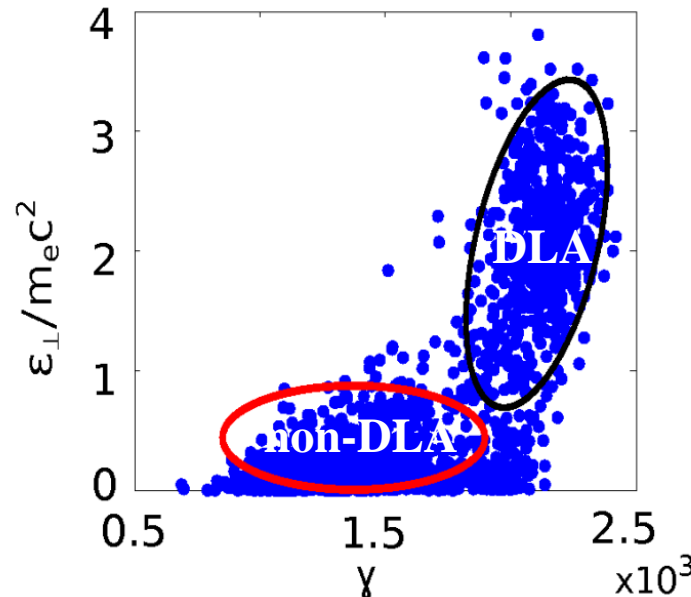
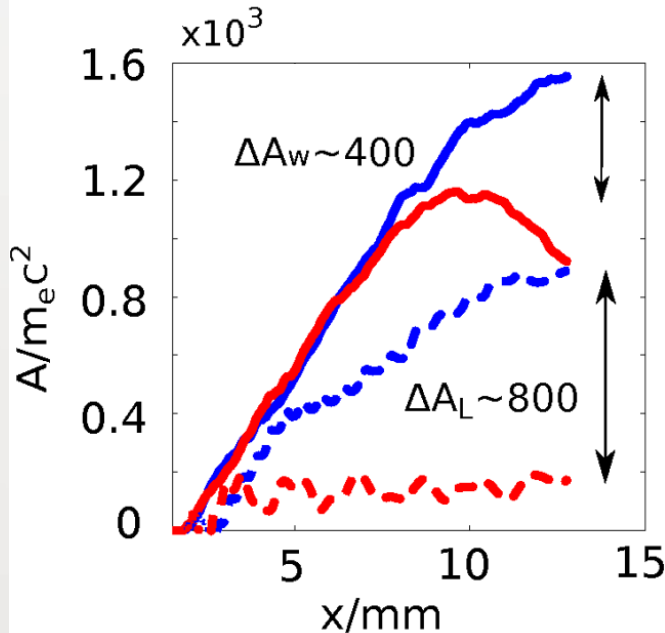
Phase space bifurcation

Two-peak spectrum separated by 400 MeV

Bifurcation is absent without DLA pulse

X. Zhang et. al. PRL 114, 184801 (2015)

# Phase Space Correlations: Key to Synergy



DLA electrons  $\rightarrow$   
strong correlation  
between total  
energy  $\gamma m c^2$  and  
transverse energy

$$\epsilon_{\perp} = \frac{p_z^2}{2\gamma m} + \frac{m\omega_p^2 z^2}{4}$$

Strong bifurcation in  $(\epsilon_{\perp}, \gamma)$  phase space

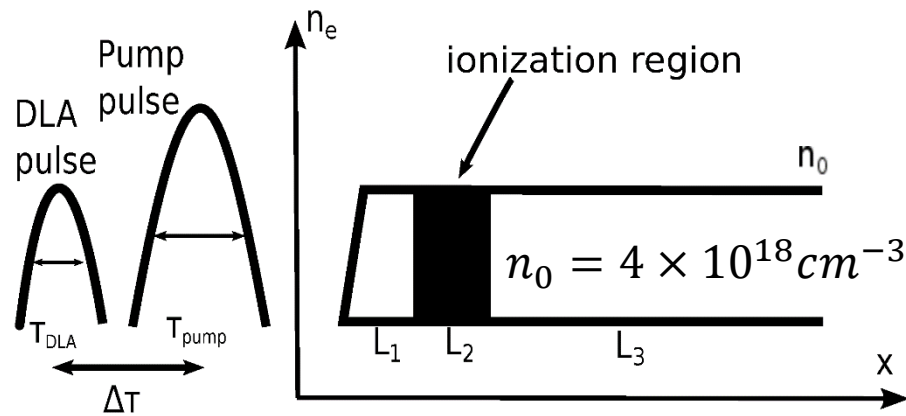
Synergy between DLA and LWFA  $\rightarrow$  higher energy  
gain from the wake for the DLA population  $\leftarrow$   
delayed dephasing!

$$\frac{d\zeta}{d(ct)} \approx \frac{1}{2\gamma_b^2} - \frac{1 + \langle p_{\perp}^2 / m_e^2 c^2 \rangle}{\gamma^2}$$

DLA electrons gain extra 200 MeV  
from the wake and extra 400 MeV  
from the laser (DLA)



# DLA is compatible with ionization injection!

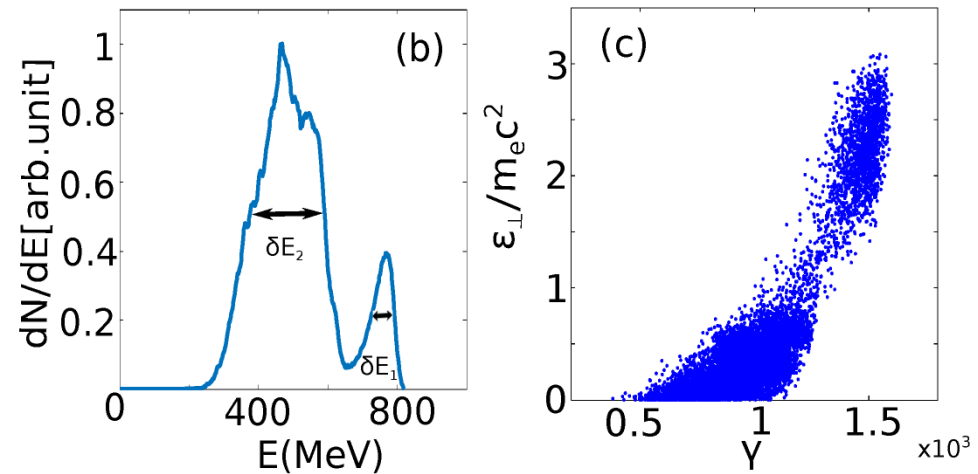
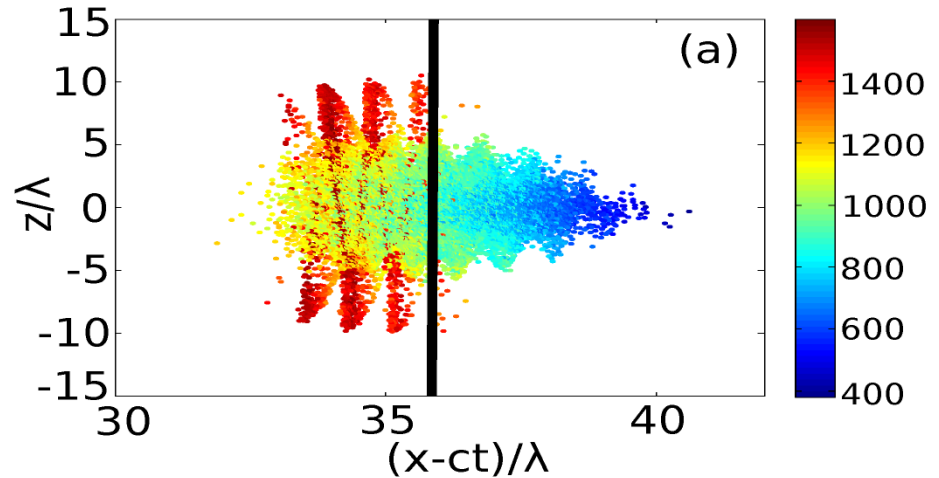


$$I_{pump} = 2.3 \times 10^{19} \text{ W/cm}^2$$

$$I_{DLA} = I_{pump}/2$$

$$U_{ion} = 870 \text{ eV} \rightarrow \text{from } O^{7+} \text{ to } O^{8+}$$

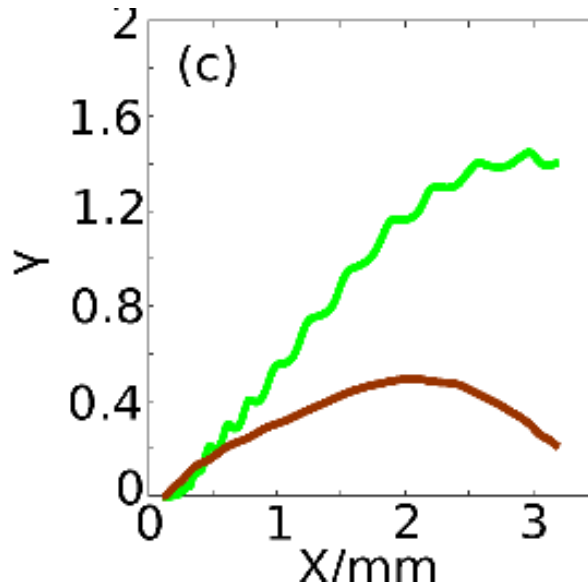
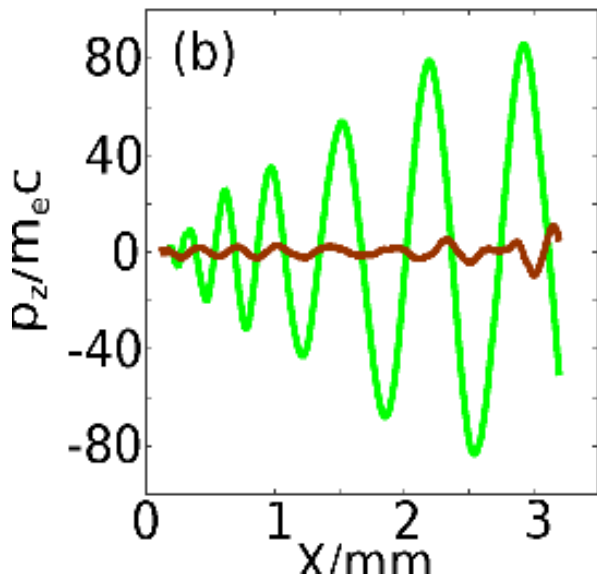
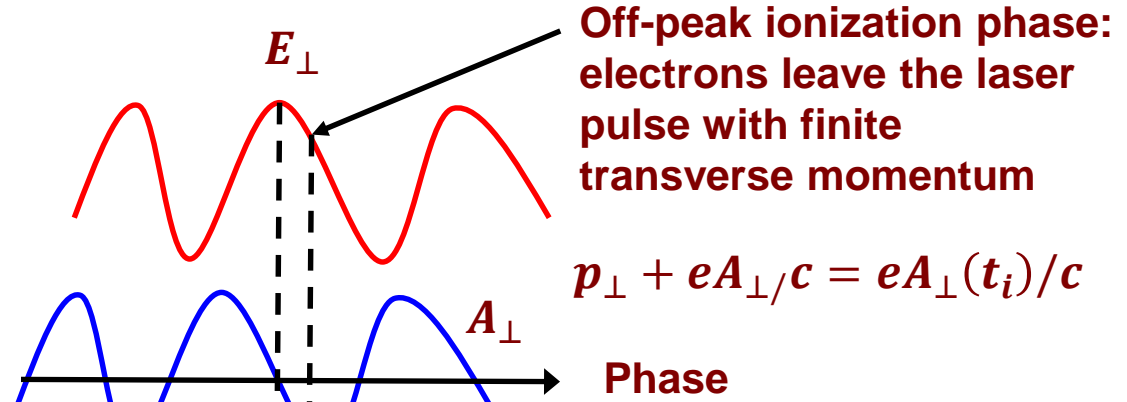
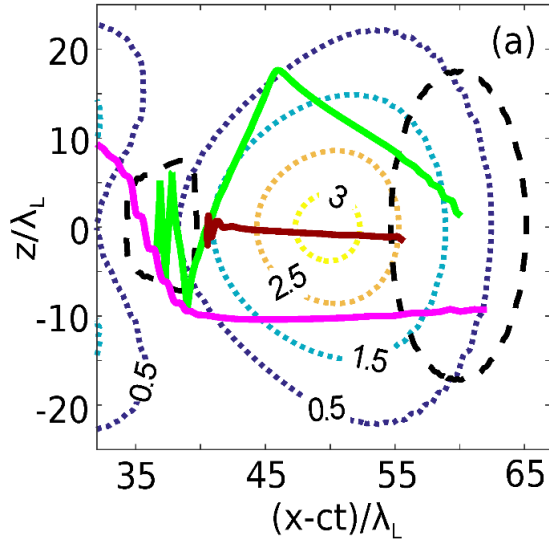
Electrons after 3mm



**Off-axis or off-peak phase ionization produces DLA electrons!**



# Off-peak phase ionization and “ricochet” DLA electrons: real atoms meet meta-atoms

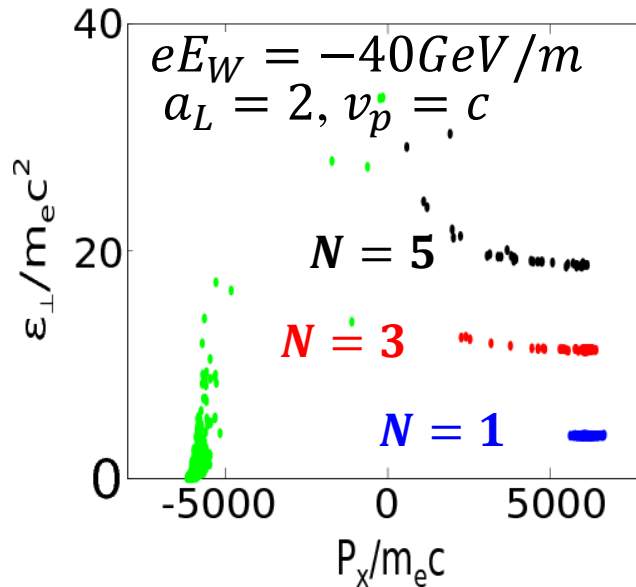
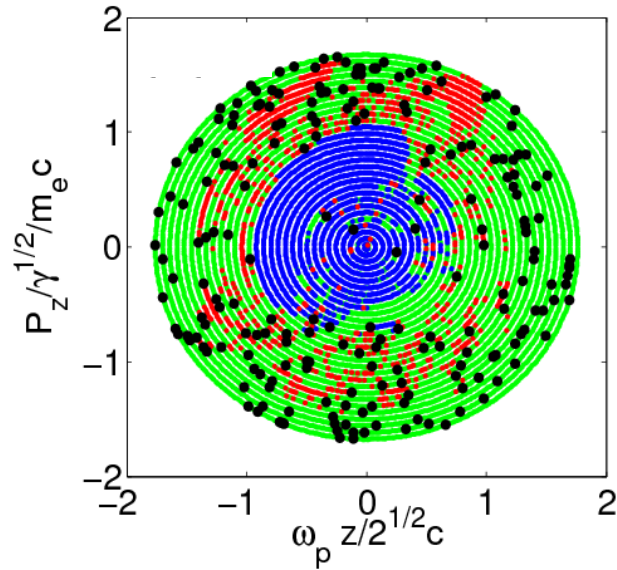


Ricochet electron starts out  
with large  $p_{\perp}$ , interacts with  
the DLA pulse  $\rightarrow$  gains even  
larger  $p_{\perp}$  and more energy



# One Step Back, Two Steps Forward: Laser Wakefield Decelerator + DLA

Initial conditions

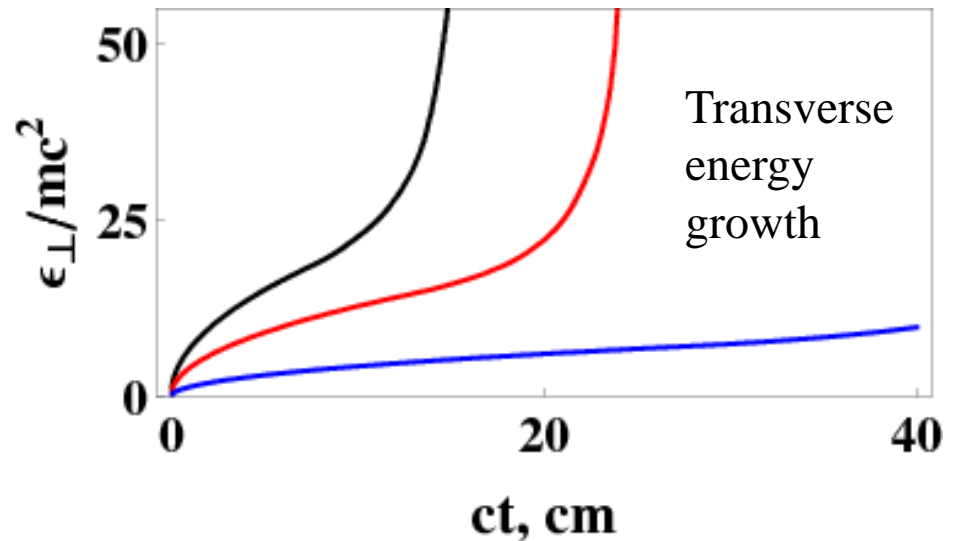
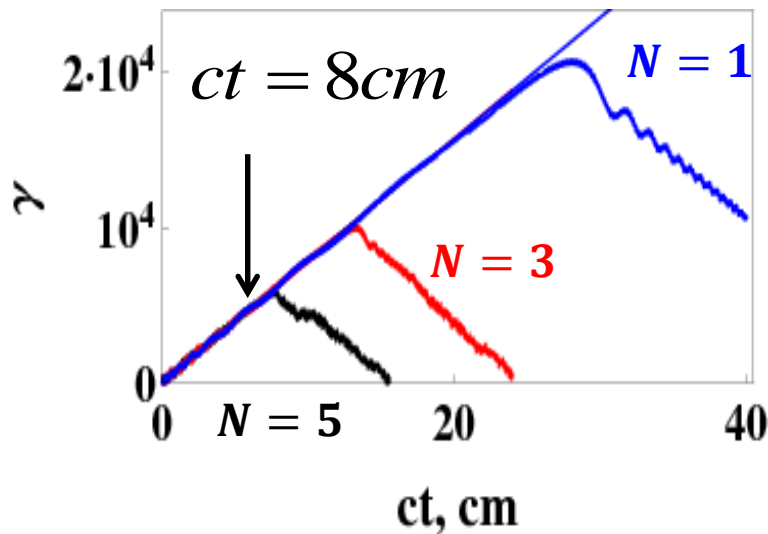


**Model: constant decelerating field  $E_W$**

**Multiple DLA harmonics:**

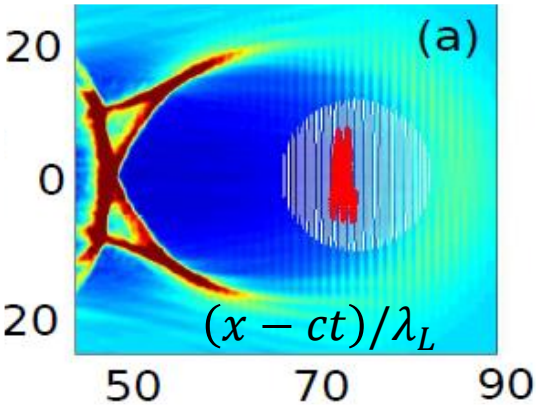
$$\omega_L \frac{1 + \langle p_z^2/m^2 c^2 \rangle}{2\gamma^2} =$$

$$= N \frac{\omega_p}{\sqrt{2}\gamma}$$

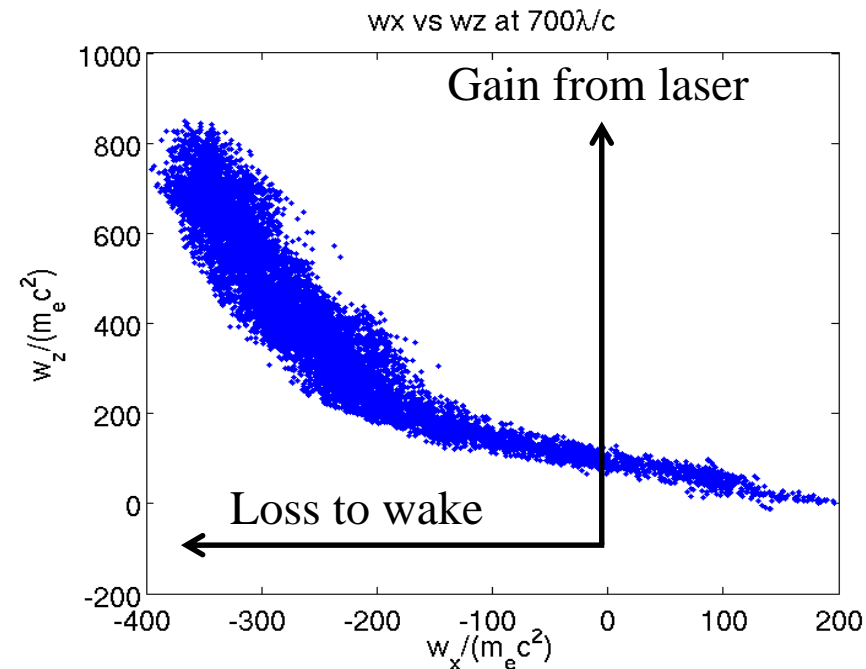
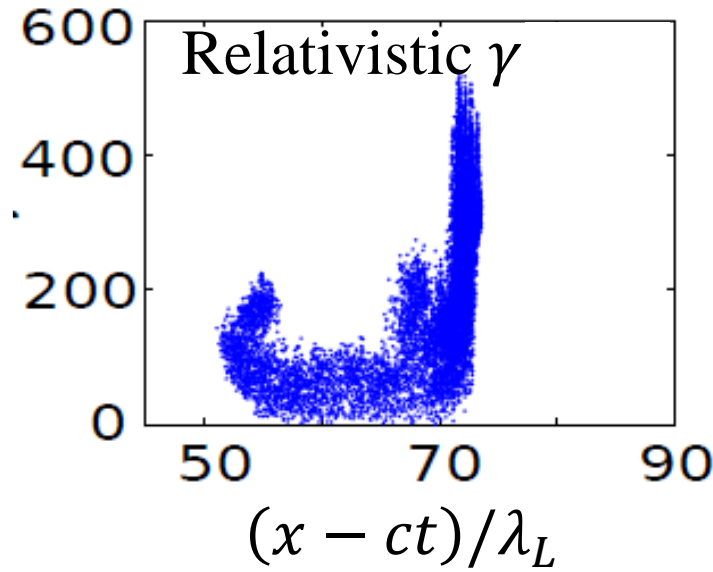




# Who needs LWFA if DLA is so great?



$\lambda_1 = 0.8 \mu\text{m}$  pulse:  
 $P_1 = 170 \text{TW}$  ( $a_1 = 6$ )  
 $\tau_1 = 35 \text{fs}$ ,  $w_1 = 12 \mu\text{m}$   
 $n_0 = 4 \times 10^{18} \text{cm}^{-3}$   
External injection into  
the decelerating phase  
 $p_{x0} = 25 m_e c$



The wake decelerates the electrons, but  
the DLA accelerates them at more than  
twice the deceleration rate!



# The mix-and-match approach to LA: the case for combining near- and mid-IR lasers

- Mid-IR lasers produce a large bubble  $r_b \sim \lambda_p \sqrt{a_L}$  because less dense plasma is used  $\rightarrow$  large-amplitude betatron oscillations are not a problem
- Vector potential  $a_L \sim \lambda_L \sqrt{I_L}$  is large for modest laser intensity
- External electron injection into a large bubble is easy
- Unique opportunity for combining a mid-IR laser pulse (“work horse” that makes a bubble) with an ultra-short solid-state laser pulse (“surgical tool” that injects electrons, excites betatron oscillations, provides DLA)

## Electric field or vector potential?

Ponderomotive potential:

$$a_L^2 \sim \lambda_L^2 I_L$$

Ionization rate of neutral gasses:

$$E_L \sim \sqrt{I_L}$$

Direct Laser

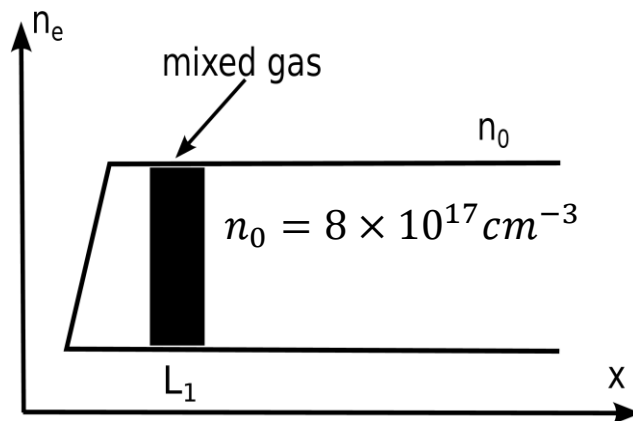
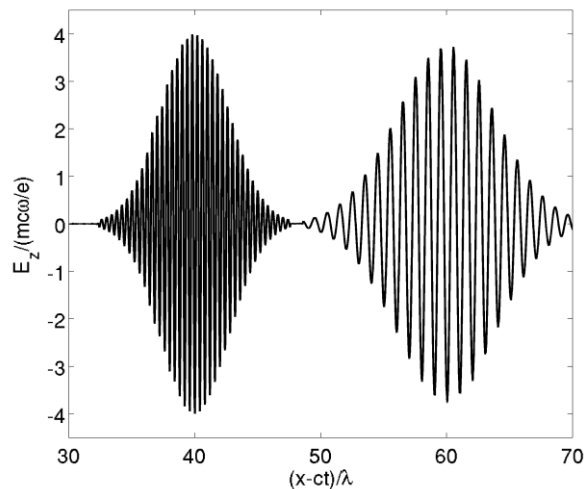
Acceleration gradient:

$$\vec{E}_L \cdot \vec{v}_\beta \sim \sqrt{I_L}$$





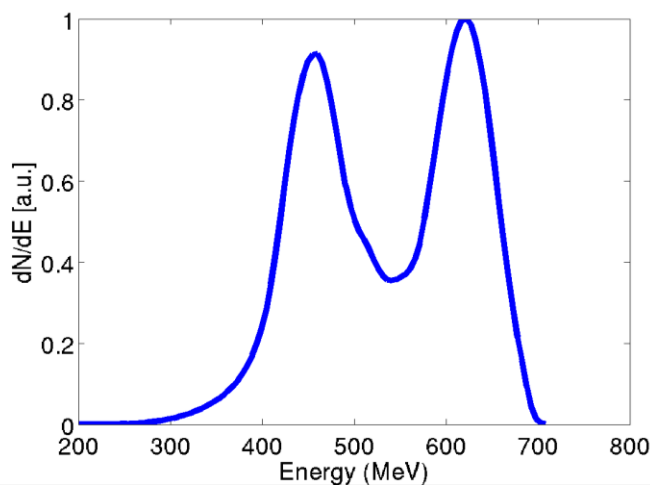
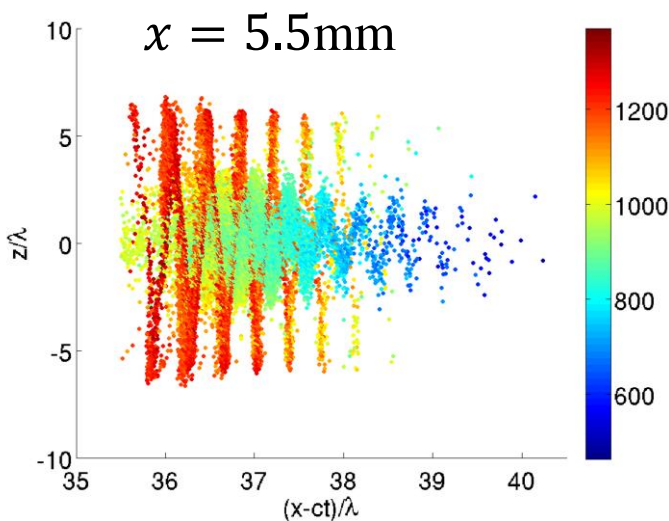
# Injection, LWFA, and DLA using a sequence of $2.0\mu m$ and a $0.8\mu m$ laser pulses



$\lambda_0 = 2\mu m$  pulse:  
 $P_0 = 65TW$  ( $a_0 = 3.7$ )  
 $\tau_0 = 45fs$ ,  $w_0 = 30\mu m$

$\lambda_1 = 0.8\mu m$  pulse:  
 $P_1 = 33TW$  ( $a_1 = 1.6$ )  
 $\tau_1 = 30fs$ ,  $w_1 = 20\mu m$

Time delay:  $\Delta t = 120fs$



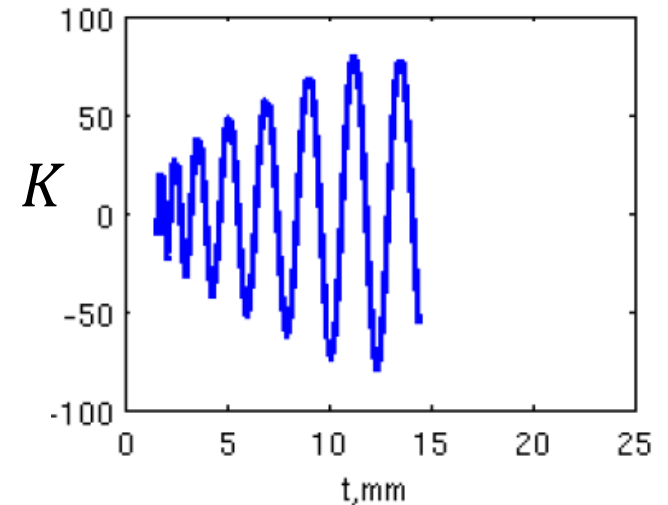
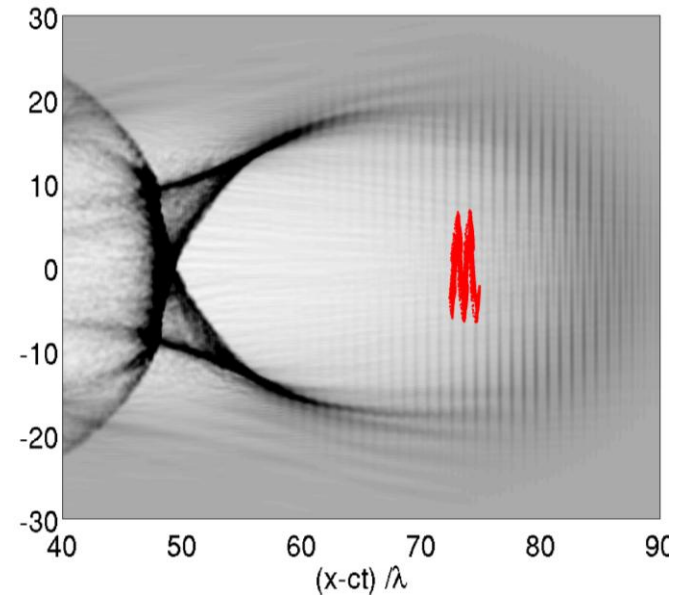
Electrons gain  
400MeV from wake  
and 200MeV from  
 $\lambda = 0.8\mu m$  laser: 1<sup>st</sup>  
harmonic DLA  
 $\omega_L(1 - v_z/v_p) = \omega_\beta$



# How the entire LPA paradigm may be changed by Direct Laser Acceleration

- Synchronization of externally injected beam is the key to injecting into the decelerating phase
- The main role of the bubble is not accelerate but to provide focusing field to undulating electrons
- Excellent source of X-ray and Gamma-ray radiation because of the large undulator parameter  $K = p_{\perp}/mc$

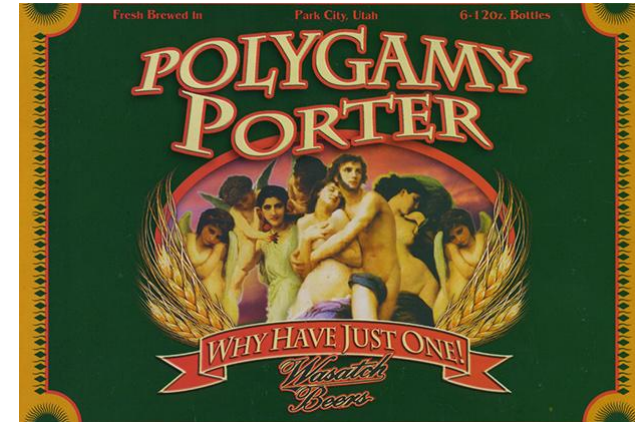
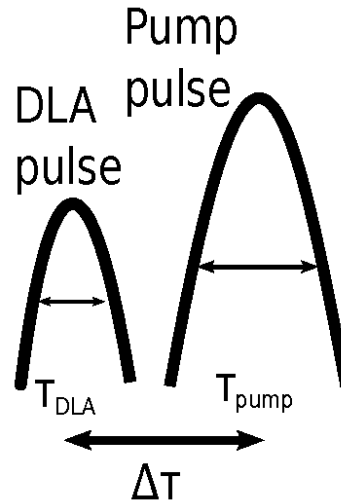
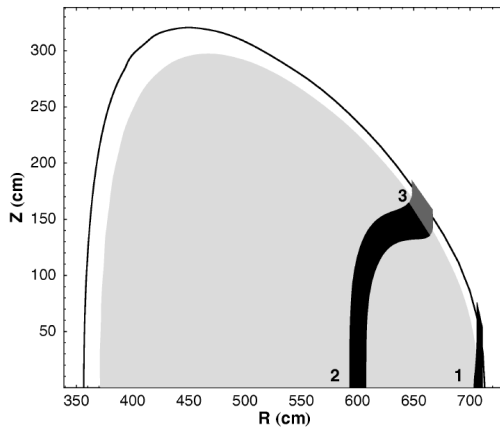
$$\omega_c \sim 2\gamma^2 \omega_{\beta} \frac{K^3}{1 + K^2} \sim K^3 \omega_L$$





# Conclusions from this talk: from the least important to the most

**When one wave doesn't do the job: bring more!**



**Watch what you are saying: people are actually listening and following!**

“Fusion is very deep but not too broad; LP is very broad but not too deep”

“Engineers use fluid descriptions. Physicists go into the phase space!”

## Happy Birthday, Nat!